

ECS 36A, April 26, 2023

Announcements

- TA's new office hours on Friday are 12:00 noon – 1:00pm
- Tutoring is available from the CS Tutoring Club

Recursion

- Sometimes it is easier to express a problem in terms of itself, but smaller
- Example: $n!$ defined as $n! = 1 \times 2 \times \dots \times n$ if $n > 0$ and $0! = 1$.
- Alternate way: $n! = n \times (n-1)!$; $0! = 1$;
- Another example: Fibonacci numbers; each number is the sum of the two preceding Fibonacci numbers:

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, ...

Structure of a Recursive Function

- Base case: this says when to stop the recursion
- Recursive case: this states the recursion part
- *Important: the recursive case must reduce the number of times the function will recurse*
 - In other words, it has to get closer to the base case

```

1: int nfact(int n)
2: {
3:     int j;
4:     int prod = 1;
5:
6:     /* special case: 0! = 1 */
7:     if (n == 0) return(1);
8:
9:     /* ordinary case: loop */
10:    for(j = 1; j <= n; j++)
11:        prod *= j;
12:
13:    /* done */
14:    return(prod);
15: }

16:
17: int main(void)
18: {
19:     int n;
20:
21:     n = nfact(4);
22:     printf("4! is %d\n", n);
23:     return(0);
24: }

```

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

```
14:
15: int main(void)
16: {
17:     int n;
18:
19:     n = nfact(4);
20:     printf("4! is %d\n", n);
21:     return(0);
22: }
```

Initial call to nfact: nfact($n \leftarrow 4$)


```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:    /* done! */
12:    return(n * x);
13: }
```

nfact(4): return to main, line 19
n = 4

nfact(n ← 4):

6: condition false, so skip

9: call nfact(4-1), or nfact(3)

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```



nfact(3): return to line 9, purple arrow
n = 3

nfact(4): return to main, line 19
n = 4

`nfact(n ← 3):`

6: condition false, so skip

9: call `nfact(3-1)`, or `nfact(2)`

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =   nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

`nfact(3):` return to line 9, red arrow
n = 2


`nfact(3):` return to line 9, purple arrow
n = 3

`nfact(4):` return to main, line 19
n = 4

nfact(n ← 2):

6: condition false, so skip

9: call nfact(2-1), or nfact(1)

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

nfact(1): return to line 9, blue arrow
n = 1

nfact(2): return to line 9, red arrow
n = 2


nfact(3): return to line 9, purple arrow
n = 3

nfact(4): return to main, line 19
n = 4

nfact(n ← 1):

6: condition false, so skip

9: call nfact(1-1), or nfact(0)

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

nfact(0): return to line 9, green arrow
n = 0

nfact(1): return to line 9, blue arrow
n = 1


nfact(2): return to line 9, red arrow
n = 2

nfact(3): return to line 9, purple arrow
n = 3

nfact(4): return to main, line 19
n = 4

`nfact(n ← 0):`

6: condition true, so return 1

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

`nfact(0):` return to line 9, green arrow
`n = 0; return 1`

`nfact(1):` return to line 9, blue arrow
`n = 1; nfact(0) = 1`

`nfact(2):` return to line 9, red arrow
`n = 2`

`nfact(3):` return to line 9, purple arrow
`n = 3`


`nfact(4):` return to main, line 19
`n = 4`

nfact(n ← 1):

6: condition false, so skip

9: call nfact(1-1), or nfact(0); nfact(0) = 1, so x = 1

12: return 1 × 1 = 1

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x =  nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

~~nfact(0): return to line 9, green arrow
n = 0; return 1~~

nfact(1): return to line 9, blue arrow
n = 1; nfact(0) = 1; return 1

nfact(2): return to line 9, red arrow
n = 2

nfact(3): return to line 9, purple arrow
n = 3

nfact(4): return to main, line 19
n = 4

nfact(n ← 2):

6: condition false, so skip

9: call nfact(2-1), or nfact(1); nfact(1) = 1, so x = 1

12: return 2 × 1 = 2

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = ↑↑ nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

~~nfact(0): return to line 9, green arrow
n = 0; return 1~~

~~nfact(1): return to line 9, blue arrow
n = 1; nfact(0) = 1; return 1~~

nfact(2): return to line 9, red arrow
n = 2; nfact(1) = 1; return 2

nfact(3): return to line 9, purple arrow
n = 3 ; nfact(2) = 2

nfact(4): return to main, line 19
n = 4

nfact(n ← 3):

6: condition false, so skip

9: call nfact(3-1), or nfact(2); nfact(2) = 2, so x = 2

12: return 3 × 2 = 6

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

~~nfact(0): return to line 9, green arrow
n = 0; return 1~~

~~nfact(1): return to line 9, blue arrow
n = 1; nfact(0) = 1; return 1~~

~~nfact(2): return to line 9, red arrow
n = 2; nfact(1) = 1; return 2~~

nfact(3): return to line 9, purple arrow
n = 3 ; nfact(2) = 2; return 6

nfact(4): return to main, line 19
n = 4

nfact(n ← 4):

6: condition false, so skip

9: call nfact(4-1), or nfact(3); nfact(3) = 6, so x = 6

12: return 4 × 6 = 24

```
1: int nfact(int n)
2: {
3:     int x;
4:
5:     /* base case: check for 0 */
6:     if (n == 0) return(1);
7:
8:     /* recurse */
9:     x = nfact(n-1);
10:
11:     /* done! */
12:     return(n * x);
13: }
```

~~nfact(0): return to line 9, green arrow
n = 0; return 1~~

~~nfact(1): return to line 9, blue arrow
n = 1; nfact(0) = 1; return 1~~

~~nfact(2): return to line 9, red arrow
n = 2; nfact(1) = 1; return 2~~

~~nfact(3): return to line 9, purple arrow
n = 3; nfact(2) = 2; return 6~~

nfact(4): return to main, line 19
n = 4; return 24


```
1: int ispal(char *n)
2: {
3:     /* base case */
4:     if (!*n || strlen(n) == 1)
5:         return(1);
6:
7:     /* recurse case */
8:     if (*n == n[strlen(n)-1]) {
9:         n[strlen(n)-1] = '\\0';
10:        return(ispal(n+1));
11:    }
12:    else return(0);
13: }
```

```
14:
15: int main(void)
16: {
17:     char buf[1000];
18:     (void) strcpy(buf, "madam")
19:     if (ispal(buf))
20:         printf("Palindrome\n");
21:     else
22:         printf("Not a palindrome\n");
23:     return(0);
24: }
```

Initial call to ispal: ispal($n \leftarrow$ "madam")

```
1: int ispal(char *n)
2: {
3:     /* base case */
4:     if (!*n || strlen(n) == 1)
5:         return(1);
6:
7:     /* recurse case */
8:     if (*n == n[strlen(n)-1]){
9:         n[strlen(n)-1] = '\\0';
10:        return(ispal(n+1));
11:    }
12:    else return(0);
13: }
```

ispal("madam"): return to main, line 19
n = "madam"

ispal(n ← "madam"):

4: condition false, so skip

9: call ispal("ada")

```
1: int ispal(char *n)
2: {
3:     /* base case */
4:     if (!*n || strlen(n) == 1)
5:         return(1);
6:
7:     /* recurse case */
8:     if (*n == n[strlen(n)-1]) {
9:         n[strlen(n)-1] = '\\0';
10:        return(ispal(n+1));
11:    }
12:    else return(0);
13: }
```

ispal("ada"): return to line 10, purple arrow

n = "ada"

ispal("madam"): return to main, line 19
n = "madam"

ispal(n ← "ada"):

6: condition false, so skip

9: call ispal("d")

```
1: int ispal(char *n)
2: {
3:     /* base case */
4:     if (!*n || strlen(n) == 1)
5:         return(1);
6:
7:     /* recurse case */
8:     if (*n == n[strlen(n)-1]) {
9:         n[strlen(n)-1] = '\\0';
10:        return(ispal(n+1));
11:    }
12:    else return(0);
13: }
```

ispal("d"): return to line 10, red arrow
n = "d"

ispal("ada"): return to line 10, purple
arrow
n = "ada"

ispal("madam"): return to main, line 19
n = "madam"

ispal(n ← "d"):
6: condition true, so return 1

```
1: int ispal(char *n)
2: {
3:     /* base case */
4:     if (!*n || strlen(n) == 1)
5:         return(1);
6:         ↑
7:     /* recurse case */
8:     if (*n == n[strlen(n)-1]) {
9:         n[strlen(n)-1] = '\\0';
10:        return(ispal(n+1));
11:    }
12:    else return(0);
13: }
```

ispal("d"): do not recurse, blue arrow

ispal("d"): return to line 10, red arrow
n = "d"

ispal("ada"): return to line 10, purple arrow
n = "ada"

ispal("madam"): return to main, line 19
n = "madam"

ispal(n ← "d"):
6: condition true, so return 1

```
1: int ispal(char *n)
2: {
3:     /* base case */
4:     if (!*n || strlen(n) == 1)
5:         return(1);
6:         ↑
7:     /* recurse case */
8:     if (*n == n[strlen(n)-1]) {
9:         n[strlen(n)-1] = '\\0';
10:        return(ispal(n+1));
11:    }
12:    else return(0);
13: }
```

~~ispal(""): line 5, returns 1~~

ispal("d"): return to line 10, red arrow
n = "d"

ispal("ada"): return to line 10, purple
arrow
n = "ada"

ispal("madam"): return to main, line 19
n = "madam"

ispal(n ← "d"):
at line 10, return 1

```
1: int ispal(char *n)
2: {
3:     /* base case */
4:     if (!*n || strlen(n) == 1)
5:         return(1);
6:
7:     /* recurse case */
8:     if (*n == n[strlen(n)-1]) {
9:         n[strlen(n)-1] = '\\0';
10:        return(ispal(n+1));
11:    }
12:    else return(0);
13: }
```

~~ispal("d"): at line 10, ispal is 1, so return 1~~

ispal("ada"): return to line 10, purple arrow

n = "ada"

ispal("madam"): return to main, line 19
n = "madam"

ispal(n ← "ada"):
at line 10, return 1

```
1: int ispal(char *n)
2: {
3:     /* base case */
4:     if (!*n || strlen(n) == 1)
5:         return(1);
6:
7:     /* recurse case */
8:     if (*n == n[strlen(n)-1]) {
9:         n[strlen(n)-1] = '\\0';
10:        return(ispal(n+1));
11:    }
12:    else return(0);
13: }
```

~~ispal("ada"): at line 10, ispal returns 1,
so this returns 1 also~~

ispal("madam"): return to main, line 19
n = "madam"

ispal(n ← "madam"):
at line 10, return 1

```
1: int ispal(char *n)
2: {
3:     /* base case */
4:     if (!*n || strlen(n) == 1)
5:         return(1);
6:
7:     /* recurse case */
8:     if (*n == n[strlen(n)-1]) {
9:         n[strlen(n)-1] = '\\0';
10:        return(ispal(n+1));
11:    }
12:    else return(0);
13: }
```

~~ispal("madam"): at line 10, ispal returns
1, so this also returns 1~~