Frequency Examination

ABCDEFGHIJKLMNOPQRSTUVWXYZ

- 1 31004011301001300112000000
- 2 1002221001301000010404000
- 3 1200000201140004013021000
- 4 2110220100001043100000211
- 5 10500021200000500030020000
- 6 0111002231101210000030101

Letter frequencies are (H high, M medium, L low):

HMMMHMMHHMMHHMLHHHMLLLL

Begin Decryption

- First matches characteristics of unshifted alphabet
- Third matches if I shifted to A
- Sixth matches if V shifted to A
- Substitute into ciphertext (bold are substitutions)

ADIYS	RIUKB	OCKKL	MI GH K	A ZO TO
EIOOL	I F T AG	PAUEF	VATAS	CI IT W
EOCNO	EIOOL	$\mathbf{B}M\mathbf{T}FV$	EGGOP	CNEKI
HS SE W	NECSE	D D AA A	RWCXS	ANSNP
H HE UL	QO NO F	E EG OS	WLPCM	AJEOC
MIUAX				

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Look For Clues

- AJE in last line suggests "are", meaning second alphabet maps A into S:
 - ALIYS RICKB OCKSL MIGHS AZOTO
 - MIOOL INTAG PACEF VATIS CIITE
 - EOCNO MIOOL BUTFV EGOOP CNESI
 - HSSEE NECSE LDAAA RECXS ANANP
 - HHECL QONON EEGOS ELPCM AREOC MICAX

Next Alphabet

• MICAX in last line suggests "mical" (a common ending for an adjective), meaning fourth alphabet maps O into A:

ALIMS	RICKP	OCKSL	AIGHS	AN O TO
MICOL	$\mathbf{INTO}\mathbf{G}$	PACET	VATIS	QIITE
ECCNO	MICOL	$\mathbf{BUTT}\mathbf{V}$	EGOOD	CNESI
VSSEE	NSCSE	LDOAA	RECL S	ANAND
HHECL	EONON	ES G OS	ELDCM	AREC C
MICAL				

Got It!

• QI means that U maps into I, as Q is always followed by U:

ALIME	RICKP	ACKSL	AUGHS	ANATO
MICAL	INTOS	PACET	HATIS	QUITE
ECONO	MICAL	BUTTH	EGOOD	ONESI
VESEE	NSOSE	LDOMA	RECLE	ANAND
THECL	EANON	ESSOS	ELDOM	ARECO
MICAL				

One-Time Pad

- A Vigenère cipher with a random key at least as long as the message
 - Provably unbreakable
 - Why? Look at ciphertext DXQR. Equally likely to correspond to plaintext DOIT (key AJIY) and to plaintext DONT (key AJDY) and any other 4 letters
 - Warning: keys *must* be random, or you can attack the cipher by trying to regenerate the key
 - Approximations, such as using pseudorandom number generators to generate keys, are *not* random

Overview of the DES

- A block cipher:
 - encrypts blocks of 64 bits using a 64 bit key
 - outputs 64 bits of ciphertext
- A product cipher
 - basic unit is the bit
 - performs both substitution and transposition (permutation) on the bits
- Cipher consists of 16 rounds (iterations) each with a round key generated from the user-supplied key

Generation of Round Keys



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Encipherment



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The f Function



Controversy

- Considered too weak
 - Diffie, Hellman said in a few years technology would allow DES to be broken in days
 - Design using 1999 technology published
 - Design decisions not public
 - S-boxes may have backdoors

Undesirable Properties

- 4 weak keys
 - They are their own inverses
- 12 semi-weak keys
 - Each has another semi-weak key as inverse
- Complementation property
 - $\text{DES}_k(m) = c \Rightarrow \text{DES}_k(m') = c'$
- S-boxes exhibit irregular properties
 - Distribution of odd, even numbers non-random
 - Outputs of fourth box depends on input to third box

Differential Cryptanalysis

- A chosen ciphertext attack
 - Requires 2⁴⁷ plaintext, ciphertext pairs
- Revealed several properties
 - Small changes in S-boxes reduce the number of pairs needed
 - Making every bit of the round keys independent does not impede attack
- Linear cryptanalysis improves result
 - Requires 2⁴³ plaintext, ciphertext pairs

DES Modes

- Electronic Code Book Mode (ECB)
 - Encipher each block independently
- Cipher Block Chaining Mode (CBC)
 - Xor each block with previous ciphertext block
 - Requires an initialization vector for the first one
- Encrypt-Decrypt-Encrypt Mode (2 keys: *k*, *k'*)

 $- c = \text{DES}_k(\text{DES}_k^{-1}(\text{DES}_k(m)))$

• Encrypt-Encrypt-Encrypt Mode (3 keys: k, k', k'') - $c = DES_k(DES_{k'}(DES_{k'}(m)))$

CBC Mode Encryption



CBC Mode Decryption



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Self-Healing Property

- Initial message
 - 3231343336353837 3231343336353837 3231343336353837 3231343336353837
- Received as (underlined 4c should be 4b)
 - ef7c<u>4c</u>b2b4ce6f3b f6266e3a97af0e2c 746ab9a6308f4256 33e60b451b09603d
- Which decrypts to
 - efca61e19f4836f1 323133336353837 3231343336353837 3231343336353837
 - Incorrect bytes underlined
 - Plaintext "heals" after 2 blocks

Current Status of DES

- Design for computer system, associated software that could break any DES-enciphered message in a few days published in 1998
- Several challenges to break DES messages solved using distributed computing
- NIST selected Rijndael as Advanced Encryption Standard, successor to DES
 - Designed to withstand attacks that were successful on DES

Public Key Cryptography

- Two keys
 - Private key known only to individual
 - Public key available to anyone
 - Public key, private key inverses
- Idea
 - Confidentiality: encipher using public key, decipher using private key
 - Integrity/authentication: encipher using private key, decipher using public one

Requirements

- 1. It must be computationally easy to encipher or decipher a message given the appropriate key
- 2. It must be computationally infeasible to derive the private key from the public key
- 3. It must be computationally infeasible to determine the private key from a chosen plaintext attack

Diffie-Hellman

- Compute a common, shared key – Called a *symmetric key exchange protocol*
- Based on discrete logarithm problem
 - Given integers *n* and *g* and prime number *p*, compute *k* such that $n = g^k \mod p$
 - Solutions known for small *p*
 - Solutions computationally infeasible as *p* grows large

Algorithm

- Constants: prime p, integer $g \neq 0, 1, p-1$
 - Known to all participants
- Anne chooses private key *kAnne*, computes public key *KAnne* = $g^{kAnne} \mod p$
- To communicate with Bob, Anne computes $Kshared = KBob^{kAnne} \mod p$
- To communicate with Anne, Bob computes $Kshared = KAnne^{kBob} \mod p$
 - It can be shown these keys are equal

Example

- Assume p = 53 and g = 17
- Alice chooses *kAlice* = 5

- Then $KAlice = 17^5 \mod 53 = 40$

- Bob chooses kBob = 7
 - Then *KBob* = $17^7 \mod 53 = 6$
- Shared key:
 - $KBob^{kAlice} \mod p = 6^5 \mod 53 = 38$
 - $KAlice^{kBob} \mod p = 40^7 \mod 53 = 38$

RSA

- Exponentiation cipher
- Relies on the difficulty of determining the number of numbers relatively prime to a large integer *n*

Background

- Totient function $\phi(n)$
 - Number of positive integers less than *n* and relatively prime to *n*
 - *Relatively prime* means with no factors in common with *n*
- Example: $\phi(10) = 4$
 - 1, 3, 7, 9 are relatively prime to 10
- Example: $\phi(21) = 12$
 - 1, 2, 4, 5, 8, 10, 11, 13, 16, 17, 19, 20 are relatively prime to 21

Algorithm

- Choose two large prime numbers *p*, *q*
 - Let n = pq; then $\phi(n) = (p-1)(q-1)$
 - Choose e < n such that e is relatively prime to $\phi(n)$.
 - Compute *d* such that $ed \mod \phi(n) = 1$
- Public key: (*e*, *n*); private key: *d*
- Encipher: $c = m^e \mod n$
- Decipher: $m = c^d \mod n$

Example: Confidentiality

- Take p = 7, q = 11, so n = 77 and $\phi(n) = 60$
- Alice chooses e = 17, making d = 53
- Bob wants to send Alice secret message HELLO (07 04 11 11 14)
 - $-07^{17} \mod 77 = 28$
 - $-04^{17} \mod 77 = 16$
 - $-11^{17} \mod 77 = 44$
 - $-11^{17} \mod 77 = 44$
 - $-14^{17} \mod 77 = 42$
- Bob sends 28 16 44 44 42

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Example

- Alice receives 28 16 44 44 42
- Alice uses private key, d = 53, to decrypt message:
 - $-28^{53} \mod 77 = 07$
 - $-16^{53} \mod 77 = 04$
 - $-44^{53} \mod 77 = 11$
 - $-44^{53} \mod 77 = 11$
 - $-42^{53} \mod 77 = 14$
- Alice translates message to letters to read HELLO
 - No one else could read it, as only Alice knows her private key and that is needed for decryption

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Example: Integrity/Authentication

- Take p = 7, q = 11, so n = 77 and $\phi(n) = 60$
- Alice chooses e = 17, making d = 53
- Alice wants to send Bob message HELLO (07 04 11 11 14) so Bob knows it is what Alice sent (no changes in transit, and authenticated)
 - $07^{53} \mod 77 = 35$
 - $04^{53} \mod 77 = 09$
 - $11^{53} \mod 77 = 44$
 - $-11^{53} \mod 77 = 44$
 - $-14^{53} \mod 77 = 49$
- Alice sends 35 09 44 44 49

Example

- Bob receives 35 09 44 44 49
- Bob uses Alice's public key, e = 17, n = 77, to decrypt message:
 - $35^{17} \mod 77 = 07$
 - $09^{17} \mod 77 = 04$
 - $44^{17} \mod 77 = 11$
 - $44^{17} \mod 77 = 11$
 - $49^{17} \mod 77 = 14$
- Bob translates message to letters to read HELLO
 - Alice sent it as only she knows her private key, so no one else could have enciphered it
 - If (enciphered) message's blocks (letters) altered in transit, would not decrypt properly

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Example: Both

- Alice wants to send Bob message HELLO both enciphered and authenticated (integrity-checked)
 - Alice's keys: public (17, 77); private: 53
 - Bob's keys: public: (37, 77); private: 13
- Alice enciphers HELLO (07 04 11 11 14):
 - $(07^{53} \mod 77)^{37} \mod 77 = 07$
 - $(04^{53} \mod 77)^{37} \mod 77 = 37$
 - $(11^{53} \mod 77)^{37} \mod 77 = 44$
 - $(11^{53} \mod 77)^{37} \mod 77 = 44$
 - $(14^{53} \mod 77)^{37} \mod 77 = 14$
- Alice sends 07 37 44 44 14

Security Services

- Confidentiality
 - Only the owner of the private key knows it, so text enciphered with public key cannot be read by anyone except the owner of the private key
- Authentication
 - Only the owner of the private key knows it, so text enciphered with private key must have been generated by the owner

More Security Services

- Integrity
 - Enciphered letters cannot be changed undetectably without knowing private key
- Non-Repudiation
 - Message enciphered with private key came from someone who knew it

Warnings

- Encipher message in blocks considerably larger than the examples here
 - If 1 character per block, RSA can be broken using statistical attacks (just like classical cryptosystems)
 - Attacker cannot alter letters, but can rearrange them and alter message meaning
 - Example: reverse enciphered message of text ON to get NO

Cryptographic Checksums

- Mathematical function to generate a set of k bits from a set of n bits (where $k \le n$).
 - k is smaller then n except in unusual circumstances
- Example: ASCII parity bit
 - ASCII has 7 bits; 8th bit is "parity"
 - Even parity: even number of 1 bits
 - Odd parity: odd number of 1 bits

Example Use

- Bob receives "10111101" as bits.
 - Sender is using even parity; 6 1 bits, so character was received correctly
 - Note: could be garbled, but 2 bits would need to have been changed to preserve parity
 - Sender is using odd parity; even number of 1
 bits, so character was not received correctly