## Extra Credit 3

Due: May 7, 2018 at 11:59pm
Points: 20

## Questions

1. (10 points) Alice enciphers messages $m$ and $m^{\prime}$ using the El Gamal cipher. Unfortunately, she uses the same random integer $k$. Eve intercepts the ciphers $C$ and $c^{\prime}$ corresponding to the two messages, respectively. She learns $m$ through various sources. But she only has the ciphertext $c^{\prime}$ corresponding to $m^{\prime}$. Show how she can get $m^{\prime}$.
2. (10 points) Assume that a cryptographic checksum function computes hashes of 128 bits. Prove that the probability is approximately 0.5 that at least one collision will occur after hashing $O\left(2^{64}\right)$ randomly selected messages.
