## January 11, 2021 Outline

Assignments: Homework \#1, due January 22
Project selection, due January 22

1. Take-Grant Protection Model
(a) Counterpoint to HRU result
(b) Symmetry of take and grant rights
(c) Islands (maximal subject-only $t g$-connected subgraphs)
(d) Bridges (as a combination of terminal and initial spans)
2. Sharing
(a) Definition: can $\bullet \operatorname{share}\left(\alpha, \mathbf{x}, \mathbf{y}, G_{0}\right)$ true iff there exists a sequence of protection graphs $G_{0}, \ldots, G_{n}$ such that $G_{0} \vdash^{*} G_{n}$ using only take, grant, create, remove rules and in $G_{n}$, there is an edge from $\mathbf{x}$ to $\mathbf{y}$ labeled $\alpha$
(b) Theorem: can $\bullet \operatorname{share}\left(r, \mathbf{x}, \mathbf{y}, G_{0}\right)$ iff there is an edge from $\mathbf{x}$ to $\mathbf{y}$ labeled $r$ in $G_{0}$, or all of the following hold:
i. there is a vertex $\mathbf{y}^{\prime}$ with an edge from $\mathbf{y}^{\prime}$ to $\mathbf{y}$ labeled $r$;
ii. there is a subject $\mathbf{y}^{\prime \prime}$ which terminally spans to $\mathbf{y}^{\prime}$, or $\mathbf{y}^{\prime \prime}=\mathbf{y}^{\prime}$;
iii. there is a subject $\mathbf{x}^{\prime}$ which initially spans to $\mathbf{x}$, or $\mathbf{x}^{\prime}=\mathbf{x}$; and
iv. there is a sequence of islands $I_{1}, \ldots, I_{n}$ connected by bridges for which $\mathbf{x}^{\prime} \in I_{1}$ and $\mathbf{y}^{\prime} \in I_{n}$.
3. Model Interpretation
(a) ACM very general, broadly applicable; Take-Grant more specific, can model fewer situations
(b) Example: shared buffer managed by trusted third party
4. Stealing
(a) Definition: can $\bullet$ steal $\left(\alpha, \mathbf{x}, \mathbf{y}, G_{0}\right)$ true iff there exists a sequence of protection graphs $G_{0}, \ldots, G_{n}$ for which the following hold simultaneously:
i. there is an edge from $\mathbf{x}$ and $\mathbf{y}$ labeled $\alpha$ in $G_{n}$;
ii. there is a sequence of rule applications $\rho_{1}$ such that $G_{i-1} \vdash G_{i}$ using $\rho_{i}$; and
iii. for all vertices $\mathbf{v}$ and $\mathbf{w}$ in $G_{i-1}, 1 \leq i<n$, if there is an edge from $\mathbf{v}$ to $\mathbf{y}$ labeled $\alpha$, then $\rho_{i}$ is not of the form " $\mathbf{v}$ grants ( $\alpha$ to $\mathbf{y}$ ) to $\mathbf{w}$ ".
(b) Theorem: can $\bullet$ steal $\left(\alpha, \mathbf{x}, \mathbf{y}, G_{0}\right)$ iff there is an edge from $\mathbf{x}$ to $\mathbf{y}$ labeled $\alpha$ in $G_{0}$, or all of the following hold:
i. there is no edge from $\mathbf{x}$ and $\mathbf{y}$ labeled $\alpha$ in $G_{0}$;
ii. there exists a subject $\mathbf{x}^{\prime}$ such that $\mathbf{x}^{\prime}=\mathbf{x}$ or $\mathbf{x}^{\prime}$ initially spans to $\mathbf{x}$;
iii. there exists a vertex $\mathbf{s}$ with an edge labeled $\alpha$ to $\mathbf{y}$ in $G_{0}$; and
iv. can $\bullet$ share ( $t, \mathbf{x}^{\prime}, \mathbf{s}, G_{0}$ ) holds.
5. Conspiracy
(a) What is of interest?
(b) Access, deletion sets
(c) Conspiracy graph
(d) Number of conspirators
