# ECS 235B Module 16 Precise and Secure Policies

## Types of Mechanisms



## Secure, Precise Mechanisms

- Can one devise a procedure for developing a mechanism that is both secure *and* precise?
  - Consider confidentiality policies only here
  - Integrity policies produce same result
- Program a function with multiple inputs and one output
  - Let *p* be a function  $p: I_1 \times ... \times I_n \rightarrow R$ . Then *p* is a program with *n* inputs  $i_k \in I_k$ ,  $1 \le k \le n$ , and one output  $r \rightarrow R$

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#### Programs and Postulates

- Observability Postulate: the output of a function encodes all available information about its inputs
  - Covert channels considered part of the output
- Example: authentication function
  - Inputs name, password; output Good or Bad
  - If name invalid, immediately print Bad; else access database
  - Problem: time output of Bad, can determine if name valid
  - This means timing is part of output

#### Protection Mechanism

• Let p be a function p:  $I_1 \times ... \times I_n \rightarrow R$ . A protection mechanism m is a function

$$m: I_1 \times \ldots \times I_n \to R \cup E$$

for which, when  $i_k \in I_k$ ,  $1 \le k \le n$ , either

- $m(i_1, ..., i_n) = p(i_1, ..., i_n)$  or
- $m(i_1, ..., i_n) \in E$ .
- E is set of error outputs
  - In above example, E = { "Password Database Missing", "Password Database Locked" }

# Confidentiality Policy

- Confidentiality policy for program *p* says which inputs can be revealed
  - Formally, for  $p: I_1 \times ... \times I_n \to R$ , it is a function  $c: I_1 \times ... \times I_n \to A$ , where  $A \subseteq I_1 \times ... \times I_n$
  - A is set of inputs available to observer
- Security mechanism is function

$$m: I_1 \times \ldots \times I_n \to R \cup E$$

• *m* is secure if and only if  $\exists m': A \rightarrow R \cup E$  such that,

$$\forall i_k \in I_k, 1 \le k \le n, m(i_1, ..., i_n) = m'(c(i_1, ..., i_n))$$

• *m* returns values consistent with *c* 

## Examples

- $c(i_1, ..., i_n) = C$ , a constant
  - Deny observer any information (output does not vary with inputs)
- $c(i_1, ..., i_n) = (i_1, ..., i_n)$ , and m' = m
  - Allow observer full access to information
- $c(i_1, ..., i_n) = i_1$ 
  - Allow observer information about first input but no information about other inputs.

#### Precision

- Security policy may be over-restrictive
  - Precision measures how over-restrictive
- $m_1$ ,  $m_2$  distinct protection mechanisms for program p under policy c
  - $m_1$  as precise as  $m_2$  ( $m_1 \approx m_2$ ) if, for all inputs  $i_1, ..., i_n$ ,  $m_2(i_1, ..., i_n) = p(i_1, ..., i_n) \Longrightarrow m_1(i_1, ..., i_n) = p(i_1, ..., i_n)$
  - $m_1$  more precise than  $m_2$  ( $m_1 \sim m_2$ ) if there is an input  $(i_1', ..., i_n')$  such that  $m_1(i_1', ..., i_n') = p(i_1', ..., i_n')$  and  $m_2(i_1', ..., i_n') \neq p(i_1', ..., i_n')$ .

# Combining Mechanisms

- $m_1$ ,  $m_2$  protection mechanisms
- $m_3 = m_1 \cup m_2$ 
  - For inputs on which  $m_1$  and  $m_2$  return same value as p,  $m_3$  does also; otherwise,  $m_3$  returns same value as  $m_1$
- Theorem: if  $m_1$ ,  $m_2$  secure, then  $m_3$  secure
  - Also,  $m_3 \approx m_1$  and  $m_3 \approx m_2$
  - Follows from definitions of secure, precise, and m<sub>3</sub>

## Existence Theorem

- For any program p and security policy c, there exists a precise, secure mechanism m\* such that, for all secure mechanisms m associated with p and c, m\* ≈ m
  - Maximally precise mechanism
  - Ensures security
  - Minimizes number of denials of legitimate actions

## Lack of Effective Procedure

- There is no effective procedure that determines a maximally precise, secure mechanism for any policy and program.
  - Sketch of proof: let policy c be constant function, and p compute function
     T(x). Assume T(x) = 0. Consider program q, where

```
z = p;
if z = 0 then y := 1 else y := 2;
halt;
```

#### Rest of Sketch

- *m* associated with *q*, *y* value of *m*, *z* output of *p* corresponding to *T*(*x*)
- $\forall x [T(x) = 0] \rightarrow m(x) = 1$
- $\exists x' [T(x') \neq 0] \rightarrow m(x) = 2 \text{ or } m(x) \text{ undefined}$
- If you can determine *m*, you can determine whether T(x) = 0 for all x
- Determines some information about input (is it 0?)
- Contradicts constancy of *c*.
- Therefore no such procedure exists

# Quiz

Which of the following are true?

- A security policy defines a set of states considered secure.
- A security mechanism is precise if it prevents the system from entering any non-secure states.
- A security mechanism is precise if it allows the system to enter nonsecure states.
- A security mechanism is precise if it allows the system to enter any secure state and not any non-secure state.