

# ECS 235B Module 31

## Role-Based Access Control

# Role-Based Access Control

- Access depends on function, not identity
  - Example:
    - Allison, bookkeeper for Math Dept, has access to financial records.
    - She leaves.
    - Betty hired as the new bookkeeper, so she now has access to those records
  - The role of “bookkeeper” dictates access, not the identity of the individual.

# Definitions

- Role  $r$ : collection of job functions
  - $trans(r)$ : set of authorized transactions for  $r$
- Active role of subject  $s$ : role  $s$  is currently in
  - $actr(s)$
- Authorized roles of a subject  $s$ : set of roles  $s$  is authorized to assume
  - $authr(s)$
- $canexec(s, t)$  iff subject  $s$  can execute transaction  $t$  at current time

# Axioms

Let  $S$  be the set of subjects and  $T$  the set of transactions.

- *Rule of role assignment:*  $(\forall s \in S)(\forall t \in T) [canexec(s, t) \rightarrow actr(s) \neq \emptyset]$ .
  - If  $s$  can execute a transaction, it has a role
  - This ties transactions to roles
- *Rule of role authorization:*  $(\forall s \in S) [actr(s) \subseteq authr(s)]$ .
  - Subject must be authorized to assume an active role (otherwise, any subject could assume any role)

# Axiom

- *Rule of transaction authorization:*

$$(\forall s \in S)(\forall t \in T) [canexec(s, t) \rightarrow t \in trans(ctr(s))].$$

- If a subject  $s$  can execute a transaction, then the transaction is an authorized one for the role  $s$  has assumed

# Containment of Roles

- Trainer can do all transactions that trainee can do (and then some).

This means role  $r$  contains role  $r'$  ( $r > r'$ ). So:

$$(\forall s \in S)[ r \in \text{authr}(s) \wedge r > r' \rightarrow r' \in \text{authr}(s) ]$$

# Separation of Duty

- Let  $r$  be a role, and let  $s$  be a subject such that  $r \in \mathit{auth}(s)$ . Then the predicate  $\mathit{meauth}(r)$  (for mutually exclusive authorizations) is the set of roles that  $s$  cannot assume because of the separation of duty requirement.
- Separation of duty:  
$$(\forall r_1, r_2 \in R) [ r_2 \in \mathit{meauth}(r_1) \rightarrow [ (\forall s \in S) [ r_1 \in \mathit{authr}(s) \rightarrow r_2 \notin \mathit{authr}(s) ] ] ]$$

# RBAC Hierarchy

- $RBAC_0$ : basic model (you just saw it)
- $RBAC_1$ : adds role hierarchies to  $RBAC_0$
- $RBAC_2$ : adds constraints to  $RBAC_0$
- $RBAC_3$ : adds both role hierarchies, constraints to  $RBAC_0$ 
  - It combines  $RBAC_1$  and  $RBAC_2$



# RBAC<sub>0</sub>, Formally

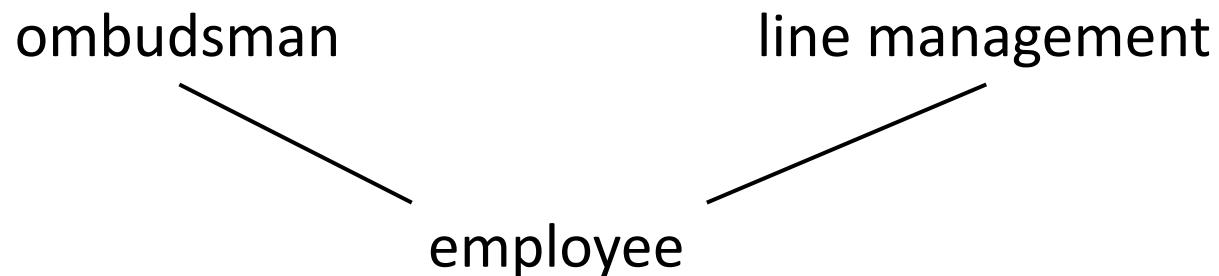
- Set of users  $U$ , roles  $R$ , permissions  $P$ , sessions  $S$
- Relation  $PA \subseteq P \times R$  mapping permissions to roles
- Relation  $UA \subseteq U \times R$  mapping users to roles
- Function  $user: S \rightarrow U$  mapping each session to a user
- Function  $roles: S \rightarrow 2^R$  mapping each session  $s \in S$  to a set of roles  $roles(s) \subseteq \{ r \in R \mid (user(s), r) \in UA \}$ , where  $s$  has permissions

$$\bigcup_{r \in roles(s)} \{ p \in P \mid (p, r) \in PA \}$$

- When a user assumes role  $r$  during session,  $r$  and hence the user assuming  $r$  gets the set of permissions associated with  $r$

# RBAC<sub>1</sub>, Intuitively

- Add containment of roles to RBAC<sub>0</sub> (this is the hierarchy)
  - It's a partial ordering
- Each role less powerful than its containing role
  - Containing role contains job functions (permissions) of the contained role
- Can define *private roles* in which one role is subordinate to two others, and those two are not related



# RBAC<sub>1</sub>, Formally

- Set of users  $U$ , roles  $R$ , permissions  $P$ , sessions  $S$
- Partial order  $RH \subseteq R \times R$ 
  - Write  $(r_1, r_2) \in RH$  as  $r_1 \geq r_2$
- Relation  $PA \subseteq P \times R$  mapping permissions to roles
- Relation  $UA \subseteq U \times R$  mapping users to roles
- Function  $user: S \rightarrow U$  mapping each session to a user
- Function  $roles: S \rightarrow 2^R$  mapping each session  $s \in S$  to a set of roles  $roles(s) \subseteq \{ r \in R \mid (\exists r' \geq r)(user(s), r') \in UA \}$ , where  $s$  has permissions
$$\bigcup_{r \in roles(s)} \{ p \in P \mid (\exists r'' \geq r)(p, r'') \in PA \}$$
  - When a user assumes role  $r$  with subordinate role  $r'$  during session,  $r$  and hence the user assuming  $r$  gets the set of permissions associated with  $r$ , and hence with  $r'$

# RBAC<sub>2</sub> and RBAC<sub>3</sub>

- RBAC<sub>2</sub> adds constraints on values that components can assume to RBAC<sub>0</sub>
  - Example: user can be in only one role at a time
  - Example: make 2 roles mutually exclusive
- RBAC<sub>3</sub> provides both role hierarchies and constraints that determine allowable values for relations and functions
  - Combines RBAC<sub>1</sub> and RBAC<sub>2</sub>
- Can be extended to manage role and privilege assignments
  - A set of administrative roles  $AR$  and permissions  $AP$  defined disjointly from  $R$  and  $P$
  - Constraints allow  $ap \in AP$  to be assigned to  $ar \in AR$  only, and  $p \in P$  to  $r \in R$  only

# Role Engineering

- *Role engineering*: defining roles and determining needed permissions
- Often used when two organizations using RBAC merge
  - Roles in one organization rarely overlap with roles in other
  - Job functions often do overlap
- *Role mining*: analyzing existing roles, permission assignments to determine optimal assignment of permissions to roles
  - *NP*-complete, but in practice optimal solutions can be approximated or produced