

# ECS 235B Module 38

## Generalized Noninterference

# Policies Changing Over Time

- Problem: previous analysis assumes static system
  - In real life, ACM changes as system commands issued
- Example:  $w \in C^*$  leads to current state
  - $cando(w, s, z)$  holds if  $s$  can execute  $z$  in current state
  - Condition noninterference on  $cando$
  - If  $\neg cando(w, \text{Lara}, \text{"write } f\text{"})$ , Lara can't interfere with any other user by writing file  $f$

# Generalize Noninterference

- $G \subseteq S$  set of subjects,  $A \subseteq Z$  set of commands,  $p$  predicate over elements of  $C^*$
- $c_s = (c_1, \dots, c_n) \in C^*$
- $\pi''(v) = v$
- $\pi''((c_1, \dots, c_n)) = (c_1', \dots, c_n')$ , where
  - $c_i' = v$  if  $p(c_1', \dots, c_{i-1}')$  and  $c_i = (s, z)$  with  $s \in G$  and  $z \in A$
  - $c_i' = c_i$  otherwise

# Intuition

- $\pi''(c_s) = c_s$
- But if  $p$  holds, and element of  $c_s$  involves both command in  $A$  and subject in  $G$ , replace corresponding element of  $c_s$  with empty command  $\nu$ 
  - Just like deleting entries from  $c_s$  as  $\pi_{A,G}$  does earlier

# Noninterference

- $G, G' \subseteq S$  sets of subjects,  $A \subseteq Z$  set of commands,  $p$  predicate over  $C^*$
- Users in  $G$  executing commands in  $A$  are *noninterfering with users in  $G'$*  under condition  $p$  iff, for all  $c_s \in C^*$  and for all  $s \in G'$ ,  $proj(s, c_s, \sigma_i) = proj(s, \pi''(c_s), \sigma_i)$ 
  - Written  $A, G :| G'$  if  $p$

# Example

- From earlier one, simple security policy based on noninterference:

$$\forall (s \in S) \forall (z \in Z) [ \{z\}, \{s\} : | S \text{ if } \neg \text{cando}(w, s, z) ]$$

- If subject can't execute command (the  $\neg \text{cando}$  part) in any state, subject can't use that command to interfere with another subject

# Another Example

- Consider system in which rights can be passed
  - $pass(s, z)$  gives  $s$  right to execute  $z$
  - $w_n = v_1, \dots, v_n$  sequence of  $v_i \in C^*$
  - $prev(w_n) = w_{n-1}; last(w_n) = v_n$

# Policy

- No subject  $s$  can use  $z$  to interfere if, in previous state,  $s$  did not have right to  $z$ , and no subject gave it to  $s$

$\{z\}, \{s\} : | S$

**if** [  $\neg cando(prev(w), s, z) \wedge [ cando(prev(w), s', pass(s, z)) \Rightarrow$   
 $\neg last(w) = (s', pass(s, z)) ] ]$



# Effect

- Suppose  $s_1 \in S$  can execute  $pass(s_2, z)$
- For all  $w \in C^*$ ,  $cando(w, s_1, pass(s_2, z))$  holds
- Initially,  $cando(v, s_2, z)$  false
- Let  $z' \in Z$  be such that  $(s_3, z')$  noninterfering with  $(s_2, z)$ 
  - So for each  $w_n$  with  $v_n = (s_3, z')$ ,  $cando(w_n, s_2, z) = cando(w_{n-1}, s_2, z)$

# Effect

- Then policy says for all  $s \in S$

$$\text{proj}(s, ((s_2, z), (s_1, \text{pass}(s_2, z)), (s_3, z'), (s_2, z)), \sigma_i) = \\ \text{proj}(s, ((s_1, \text{pass}(s_2, z)), (s_3, z'), (s_2, z)), \sigma_i)$$

- So  $s_2$ 's first execution of  $z$  does not affect any subject's observation of system