

Listing Permutations Done Recursively

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MHI 289I, Fall Quarter 2025

The Recursive n! Program

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow []$ (line 4)
- $i \leftarrow 0$ (line 5)
- $remlst \leftarrow ['b', 'c']$ (line 6)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow []$ (line 4)
- $i \leftarrow 0$ (line 5)
- $remlst \leftarrow ['b', 'c']$ (line 6)
- *call to perm*($['b', 'c']$) (line 7)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
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7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['b', 'c']): return to line 7
 $lst = ['b', 'c']$

perm(['a', 'b', 'c']): return to main program
 $lst = ['a', 'b', 'c']$

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow []$ (line 4)
- $i \leftarrow 0$ (line 5)
- $remlst \leftarrow ['b', 'c']$ (line 6)
- *call to perm*($['b', 'c']$) (line 7)
 - $intlst \leftarrow []$ (line 4)
 - $i \leftarrow 0$ (line 5)
 - $remlst \leftarrow ['c']$ (line 6)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
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4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['b', 'c']): return to line 7
 $lst = ['b', 'c']$

perm(['a', 'b', 'c']): return to main program
 $lst = ['a', 'b', 'c']$

Initial call to perm: perm(lst ← ['a', 'b', 'c'])

- intlst ← [] (line 4)
- i ← 0 (line 5)
- remlst ← ['b', 'c'] (line 6)
- call to perm(['b', 'c']) (line 7)
 - intlst ← [] (line 4)
 - i ← 0 (line 5)
 - remlst ← ['c'] (line 6)
 - call to perm(['c']) (line 7)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['c']): return to line 7
lst = ['c']

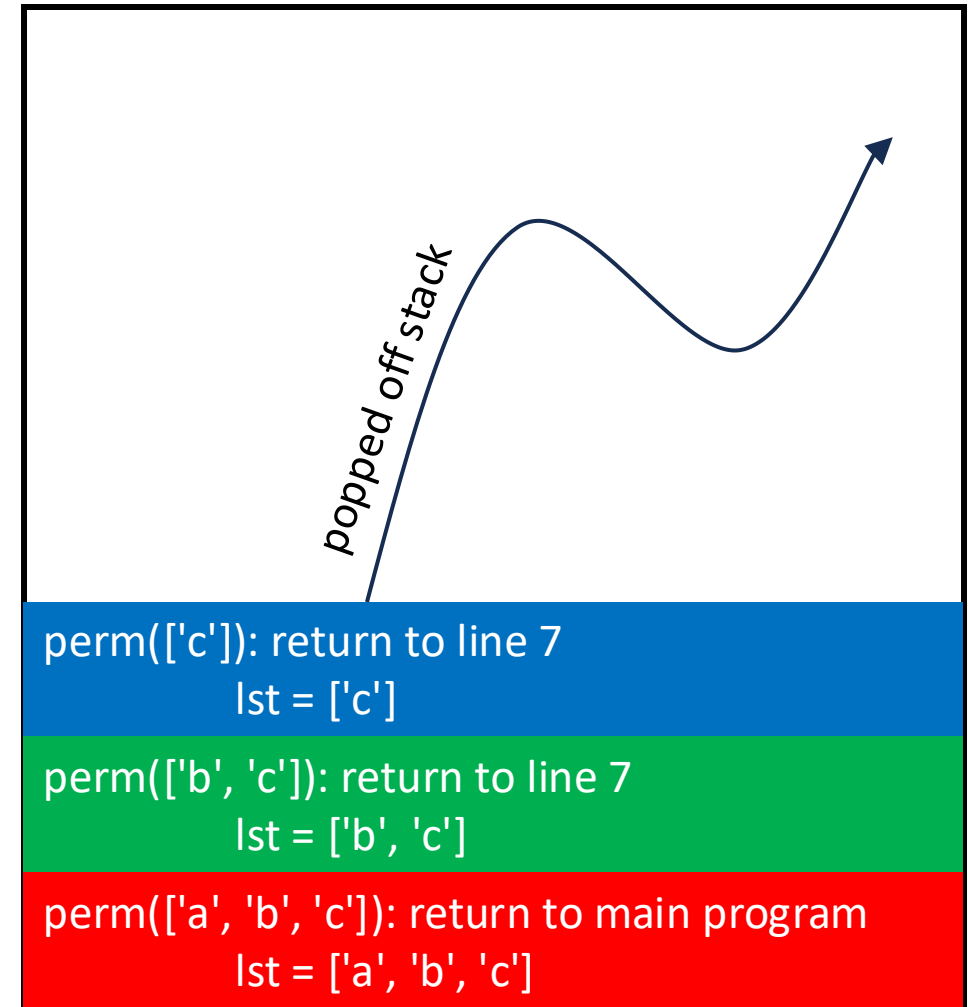
perm(['b', 'c']): return to line 7
lst = ['b', 'c']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow []$ (line 4)
- $i \leftarrow 0$ (line 5)
- $remlst \leftarrow ['b', 'c']$ (line 6)
- call to perm($['b', 'c']$) (line 7)
 - $intlst \leftarrow []$ (line 4)
 - $i \leftarrow 0$ (line 5)
 - $remlst \leftarrow ['c']$ (line 6)
 - call to perm($['c']$) (line 7)
 - as $len(lst) = 1$, returns $[['c']]$ (line 3)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```



Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow []$ (line 4)
- $i \leftarrow 0$ (line 5)
- $remlst \leftarrow ['b', 'c']$ (line 6)
- *call to perm*($['b', 'c']$) (line 7)
 - $i \leftarrow 0$ (line 5)
 - $remlst \leftarrow ['c']$ (line 6)
 - $p \leftarrow ['c']$ (line 7)
 - $intlst \leftarrow [['b'] + ['c']]$ or $[['b', 'c']]$

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['b', 'c']): return to line 7
 $lst = ['b', 'c']$

perm(['a', 'b', 'c']): return to main program
 $lst = ['a', 'b', 'c']$

Initial call to perm: perm(lst ← ['a', 'b', 'c'])

- intlst ← [] (line 4)
- i ← 0 (line 5)
- remlst ← ['b', 'c'] (line 6)
- call to perm(['b', 'c']) (line 7)
 - intlst ← [['b', 'c']]
 - i ← 1 (line 5)
 - remlst ← ['b'] (line 6)
 - call to perm(['b']) (line 7)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['b']): return to line 7
lst = ['b']

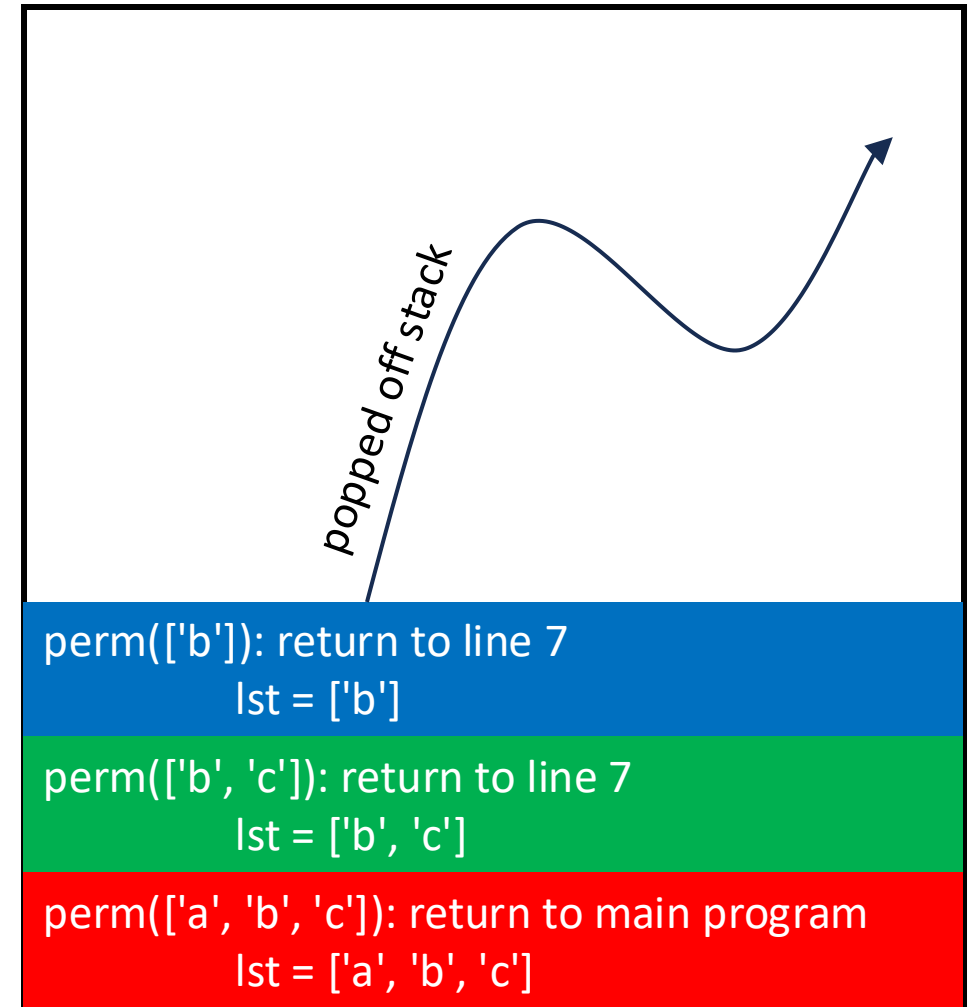
perm(['b', 'c']): return to line 7
lst = ['b', 'c']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow []$ (line 4)
- $i \leftarrow 0$ (line 5)
- $remlst \leftarrow ['b', 'c']$ (line 6)
- *call to perm*($['b', 'c']$) (line 7)
 - $intlst \leftarrow [['b', 'c']]$ (see slide 7)
 - $i \leftarrow 1$ (line 5)
 - $remlst \leftarrow ['b']$ (line 6)
 - *call to perm*($['b']$) (line 7)
 - as $len(lst) = 1$, returns $[['b']]$ (line 3)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```



Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow []$ (line 4)
- $i \leftarrow 0$ (line 5)
- $remlst \leftarrow ['b', 'c']$ (line 6)
- *call to perm*($['b', 'c']$) (line 7)
 - $i \leftarrow 1$ (line 5)
 - $remlst \leftarrow ['b']$ (line 6)
 - $p \leftarrow ['b']$
 - $intlst \leftarrow [['b', 'c'], ['c'] + ['b']] \text{ or } [['b', 'c'], ['c', 'b']]$ (line 9)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

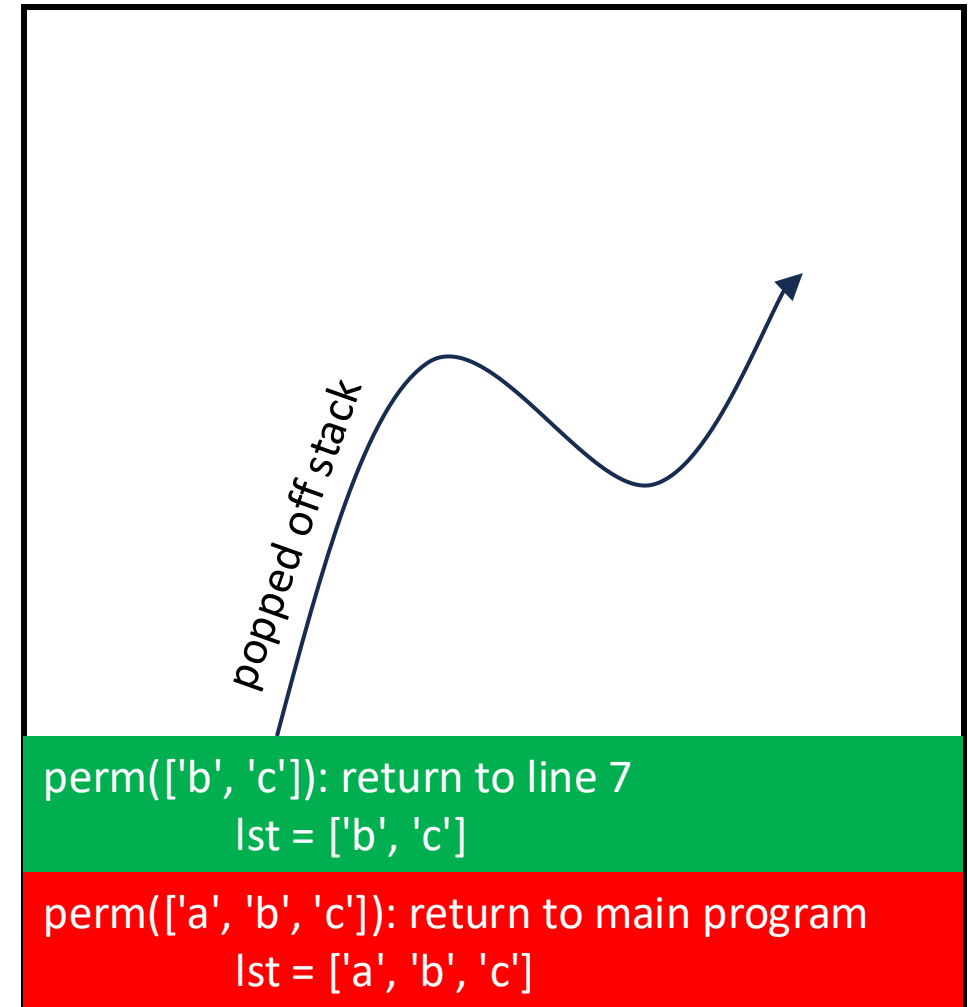
perm(['b', 'c']): return to line 7
lst = ['b', 'c']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow []$ (line 4)
- $i \leftarrow 0$ (line 5)
- $remlst \leftarrow ['b', 'c']$ (line 6)
- call to perm($['b', 'c']$) (line 7)
 - returns $[['b', 'c'], ['c', 'b']]$

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```



Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $i \leftarrow 0$ (line 5)
- $remlst \leftarrow ['b', 'c']$ (line 6)
- $p \leftarrow [['b', 'c'], ['c', 'b']]$ (line 7)
- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a']]$

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a']]$
- $i \leftarrow 1$ (line 5)
- $remlst \leftarrow ['a', 'c']$ (line 6)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a']]$
- $i \leftarrow 1$ (line 5)
- $remlst \leftarrow ['a', 'c']$ (line 6)
- *call to perm*($['a', 'c']$) (line 7)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
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7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a', 'c']): return to line 7
lst = ['a', 'c']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm(lst ← ['a', 'b', 'c'])

- intlst ← [['b', 'c', 'a'], ['c', 'b', 'a']]
- i ← 1 (line 5)
- remlst ← ['a', 'c'] (line 6)
- call to perm(['a', 'c']) (line 7)
 - intlst ← [] (line 4)
 - i ← 0 (line 5)
 - remlst ← ['c'] (line 6)
 - call to perm(['c']) (line 7)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['c']): return to line 7
lst = ['c']

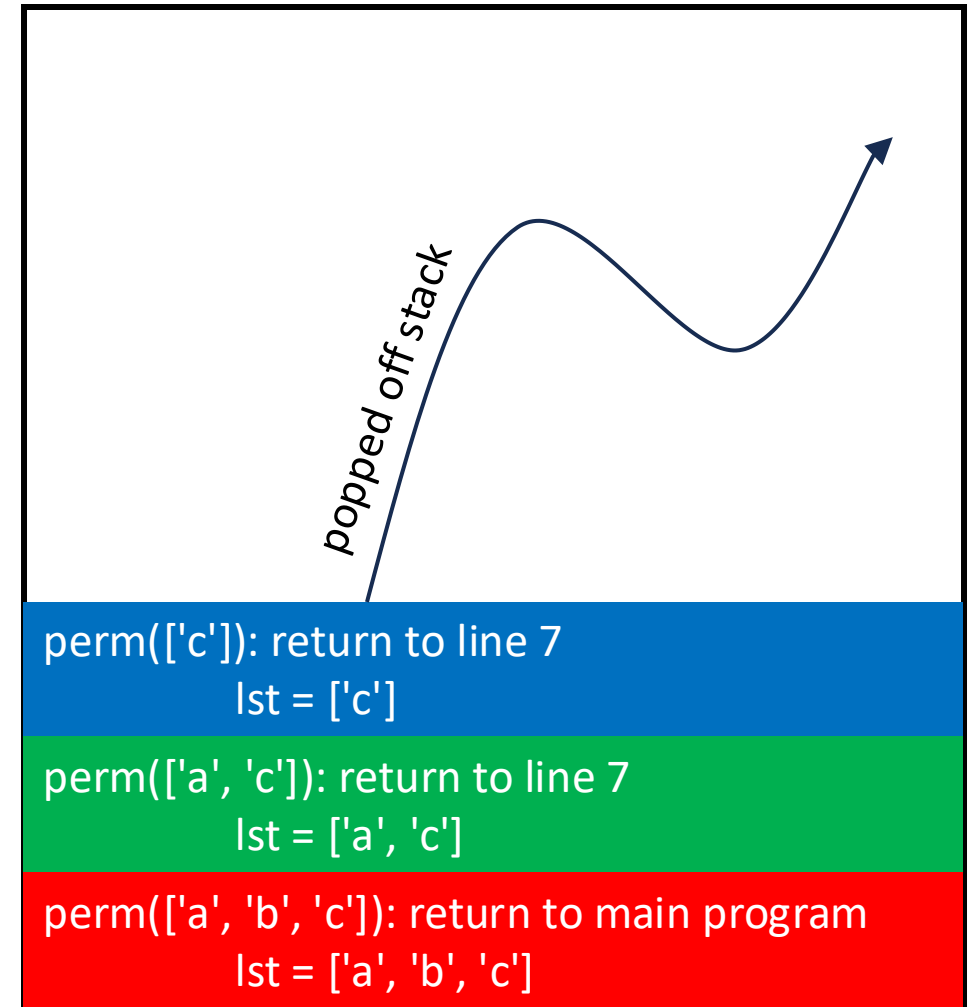
perm(['a', 'c']): return to line 7
lst = ['a', 'c']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a']]$
- $i \leftarrow 1$ (line 5)
- $remlst \leftarrow ['a', 'c']$ (line 6)
- call to perm($['a', 'c']$) (line 7)
 - $intlst \leftarrow []$ (line 4)
 - $i \leftarrow 0$ (line 5)
 - $remlst \leftarrow ['c']$ (line 6)
 - call to perm($['c']$) (line 7)
 - as $len(lst) = 1$, returns $[['c']]$ (line 3)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```



Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a']]$
- $i \leftarrow 1$ (line 5)
- $remlst \leftarrow ['a', 'c']$ (line 6)
- *call to perm*($['a', 'c']$) (line 7)
 - $i \leftarrow 0$ (line 5)
 - $remlst \leftarrow ['c']$ (line 6)
 - $p \leftarrow ['c']$ (line 7)
 - $intlst \leftarrow [['a'] + ['c']]$ *or* $[['a', 'c']]$ (line 9)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a', 'c']): return to line 7
lst = ['a', 'c']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm(lst ← ['a', 'b', 'c'])

- intlst ← [['b', 'c', 'a'], ['c', 'b', 'a']]
- i ← 1 (line 5)
- remlst ← ['a', 'c'] (line 6)
- call to perm(['a', 'c']) (line 7)
 - intlst ← [['a', 'c']]
 - i ← 1 (line 5)
 - remlst ← ['a'] (line 6)
 - call to perm(['a']) (line 7)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a']): return to line 7
lst = ['a']

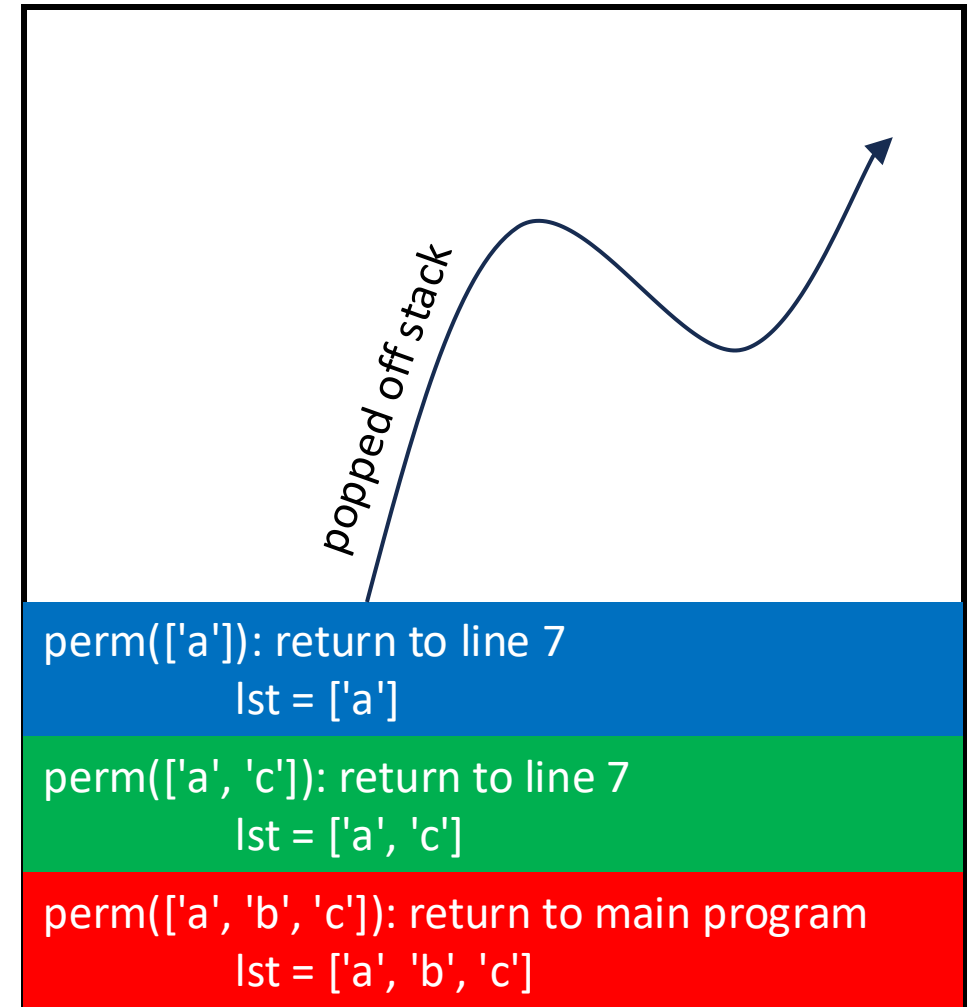
perm(['a', 'c']): return to line 7
lst = ['a', 'c']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a']]$
- $i \leftarrow 1$ (line 5)
- $remlst \leftarrow ['a', 'c']$ (line 6)
- call to perm($['a', 'c']$) (line 7)
 - $intlst \leftarrow [['a', 'c']]$ (line 9)
 - $i \leftarrow 1$ (line 5)
 - $remlst \leftarrow ['a']$ (line 6)
 - call to perm($['a']$) (line 7)
 - as $len(lst) = 1$, returns $[['a']]$ (line 3)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```



Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a']]$
- $i \leftarrow 1$ (line 5)
- $remlst \leftarrow ['a', 'c']$ (line 6)
- *call to perm*($['a', 'c']$) (line 7)
 - $i \leftarrow 1$ (line 5)
 - $remlst \leftarrow ['a']$ (line 6)
 - $p \leftarrow ['a']$ (line 7)
 - $intlst \leftarrow [['a', 'c'], ['c'] + ['a']]$ or $[['a', 'c'], ['c', 'a']]$

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

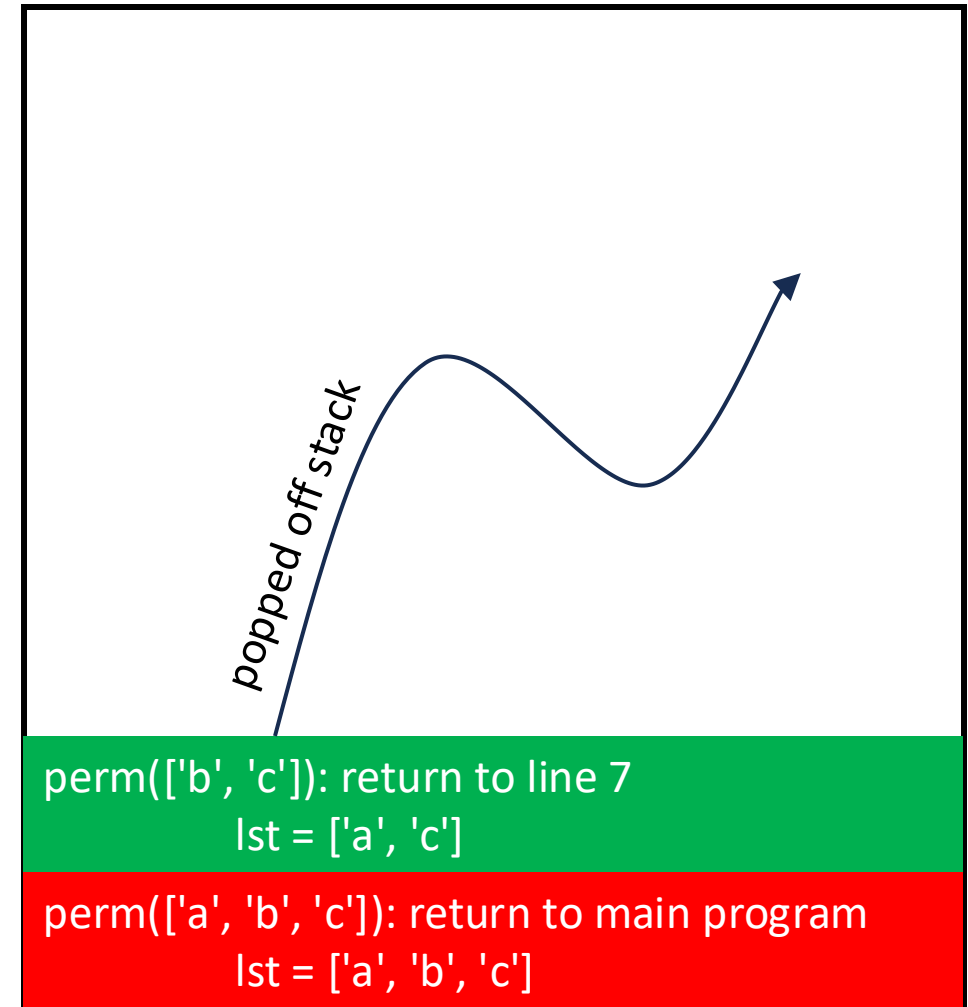
perm(['a', 'c']): return to line 7
lst = ['a', 'c']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a']]$
- $i \leftarrow 1$ (line 5)
- $remlst \leftarrow ['a', 'c']$ (line 6)
- call to perm($['a', 'c']$) (line 7)
 - return $[['a', 'c'], ['c', 'a']]$

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```



Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]$
- $i \leftarrow 2$ (line 5)
- $remlst \leftarrow ['a', 'b']$ (line 6)
- *call* perm($['a', 'b']$)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a', 'b']): return to line 7
lst = ['a', 'c']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]$
- $i \leftarrow 2$ (line 5)
- $remlst \leftarrow ['a', 'b']$ (line 6)
- *call* perm($['a', 'b']$)
 - $intlst \leftarrow []$ (line 4)
 - $i \leftarrow 0$ (line 5)
 - $remlst \leftarrow ['b']$ (line 6)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a', 'b']): return to line 7
lst = ['a', 'b']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm(lst ← ['a', 'b', 'c'])

- intlst ← [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]
- i ← 2 (line 5)
- remlst ← ['a', 'b'] (line 6)
- call perm(['a', 'b'])
 - intlst ← [] (line 4)
 - i ← 0 (line 5)
 - remlst ← ['b'] (line 6)
 - call to perm(['b']) (line 7)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['b']): return to line 7
lst = ['b']

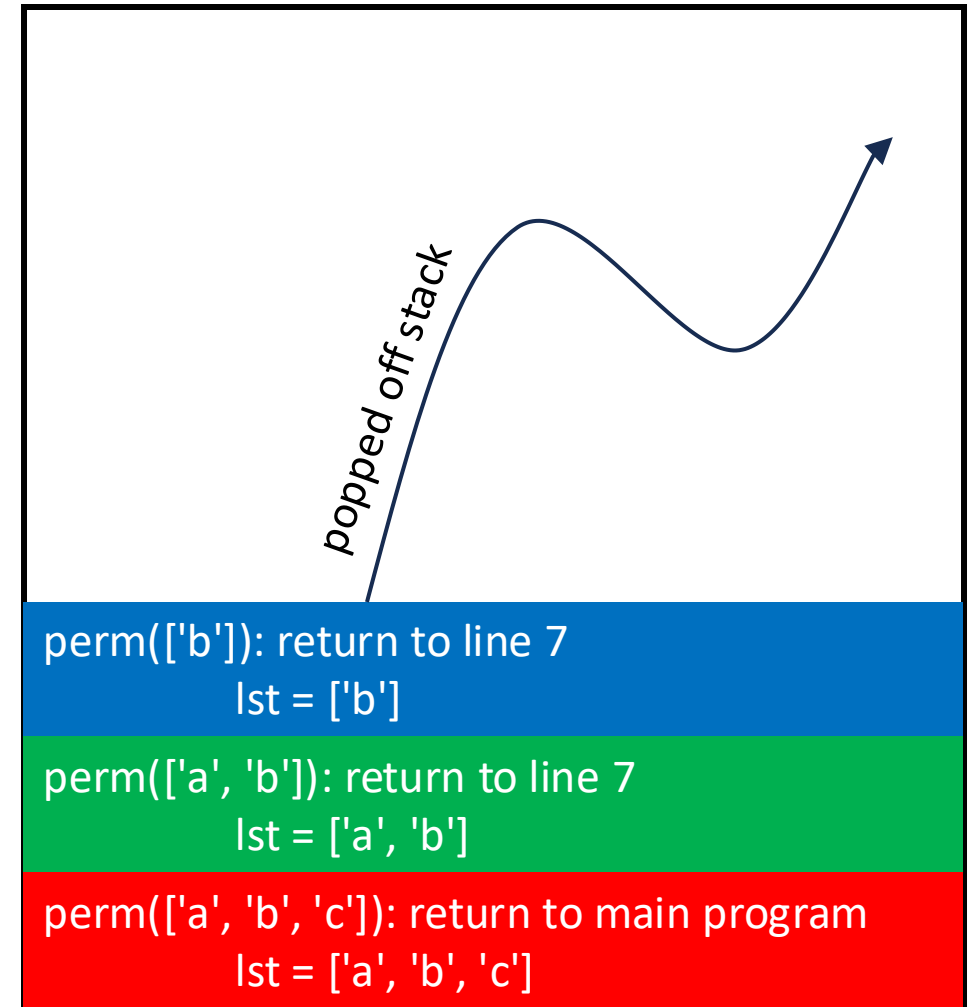
perm(['a', 'b']): return to line 7
lst = ['a', 'b']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: $\text{perm}(\text{lst} \leftarrow ['a', 'b', 'c'])$

- $\text{intlst} \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]$
- $i \leftarrow 2$ (line 5)
- $\text{remlst} \leftarrow ['a', 'b']$ (line 6)
- *call* $\text{perm}(['a', 'b'])$
 - $\text{intlst} \leftarrow []$ (line 4)
 - $i \leftarrow 0$ (line 5)
 - $\text{remlst} \leftarrow ['b']$ (line 6)
 - as $\text{len}(\text{lst}) = 1$, returns $[['b']]$ (line 3)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```



Initial call to perm: $\text{perm}(\text{lst} \leftarrow ['a', 'b', 'c'])$

- $\text{intlst} \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]$
- $i \leftarrow 2$ (line 5)
- $\text{remlst} \leftarrow ['a', 'b']$ (line 6)
- *call* $\text{perm}(['a', 'b'])$
 - $i \leftarrow 0$ (line 5)
 - $\text{remlst} \leftarrow ['b']$ (line 6)
 - *call to* $\text{perm}(['b'])$ (line 7)
 - $\text{intlst} \leftarrow [['a'] + ['b']]$ *or* $[['a', 'b']]$ (line 9)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

$\text{perm}(['a', 'b'])$: return to line 7
 $\text{lst} = ['a', 'b']$

$\text{perm}(['a', 'b', 'c'])$: return to main program
 $\text{lst} = ['a', 'b', 'c']$

Initial call to perm: perm(lst $\leftarrow$ ['a', 'b', 'c'])

- intlst $\leftarrow$ [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]
- i $\leftarrow$ 2 (line 5)
- remlst $\leftarrow$ ['a', 'b'] (line 6)
- call perm(['a', 'b'])
 - intlst $\leftarrow$ [['a', 'b']] (see previous slide)
 - i $\leftarrow$ 1 (line 5)
 - remlst $\leftarrow$ ['a'] (line 6)
 - call to perm(['a']) (line 7)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a']): return to line 7
lst = ['a']

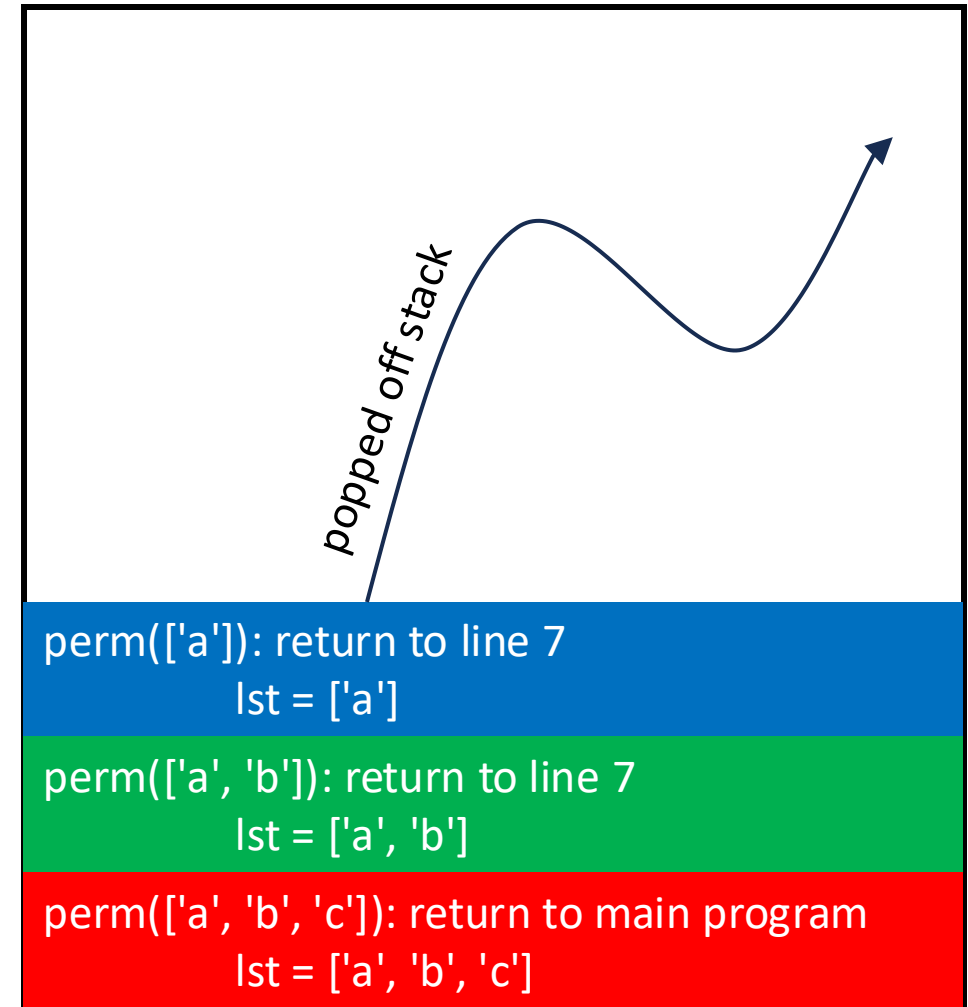
perm(['a', 'b']): return to line 7
lst = ['a', 'b']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]$
- $i \leftarrow 2$ (line 5)
- $remlst \leftarrow ['a', 'b']$ (line 6)
- *call* perm($['a', 'b']$)
 - $intlst \leftarrow [['a', 'b']]$ (see previous slide)
 - $i \leftarrow 1$ (line 5)
 - $remlst \leftarrow ['a']$ (line 6)
 - *call to* perm($['a']$) (line 7)
 - as $len(lst) = 1$, returns $[['a']]$ (line 3)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```



Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- $intlst \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]$
- $i \leftarrow 2$ (line 5)
- $remlst \leftarrow ['a', 'b']$ (line 6)
- *call* perm($['a', 'b']$)
 - $i \leftarrow 1$ (line 5)
 - $remlst \leftarrow ['a']$ (line 6)
 - $intlst \leftarrow [['a', 'b'], ['b'] + ['a']]$ or $[['a', 'b'], ['b', 'a']]$ (line 9)

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

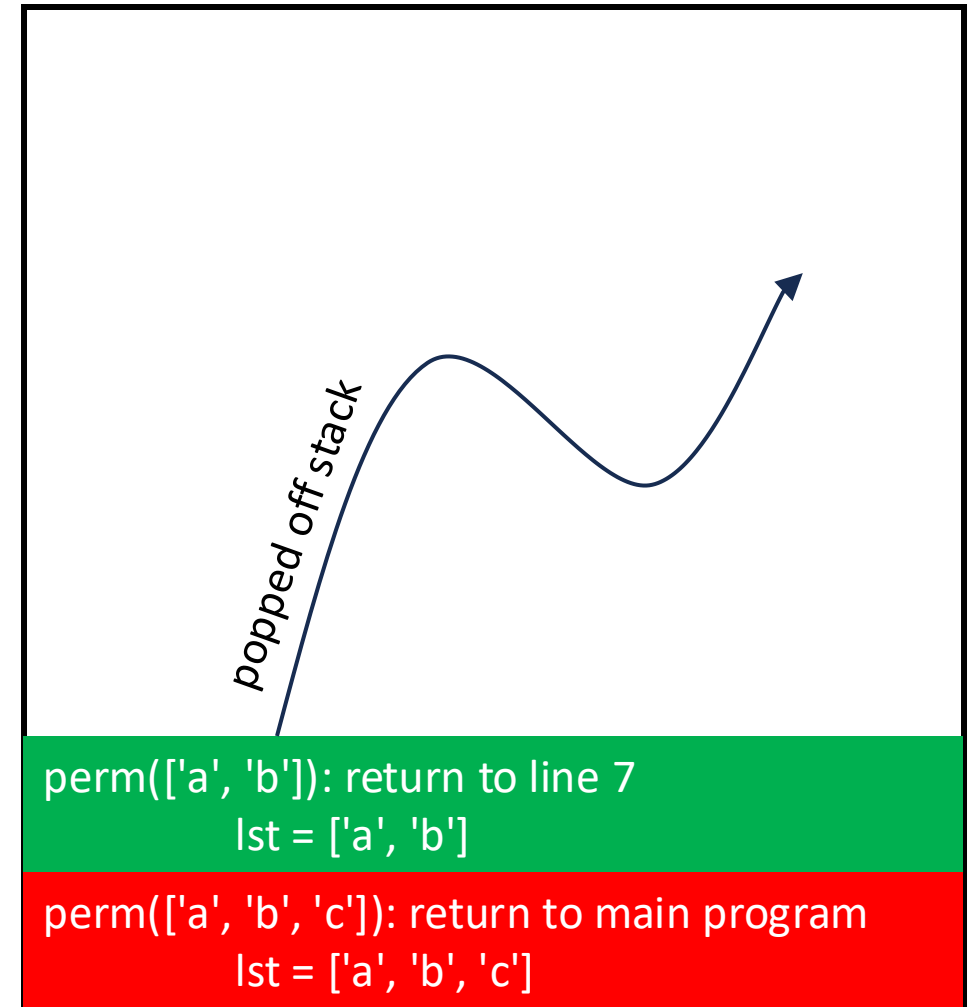
perm(['a', 'b']): return to line 7
lst = ['a', 'b']

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: $\text{perm}(\text{lst} \leftarrow ['a', 'b', 'c'])$

- $\text{intlst} \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]$
- $i \leftarrow 2$ (line 5)
- $\text{remlst} \leftarrow ['a', 'b']$ (line 6)
- *call* $\text{perm}(['a', 'b'])$
 - returns $[['a', 'b'], ['b', 'a']]$

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```



Initial call to perm: perm($lst \leftarrow ['a', 'b', 'c']$)

- returns $[['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b'], ['a', 'b', 'c'], ['b', 'a', 'c']]$

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

perm(['a', 'b', 'c']): return to main program
lst = ['a', 'b', 'c']

Initial call to perm: $\text{perm}(\text{lst} \leftarrow ['a', 'b', 'c'])$

- $\text{intlst} \leftarrow [['b', 'c', 'a'], ['c', 'b', 'a'], ['a', 'c', 'b'], ['c', 'a', 'b']]$
- $i \leftarrow 2$ (line 5)
- $\text{remlst} \leftarrow ['a', 'b']$ (line 6)
- *call* $\text{perm}(['a', 'b'])$
 - returns $[['a', 'b'], ['b', 'a']]$

```
1: def perm(lst):
2:     if len(lst) == 0: return [ ]
3:     if len(lst) == 1: return [ lst ]
4:     intlst = [ ]
5:     for i in range(len(lst)):
6:         remlst = lst[:i] + lst[i+1:]
7:         for p in perm(remlst):
8:             intlst.append([ lst[i] + p])
9:     return intlst
```

